

Math 290 ELEMENTARY LINEAR ALGEBRA

SOLUTION FOR QUIZ – I (09/20)

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[I] (20pts) List up all possible 3×6 reduced row echelon forms. Use ‘*’ to denote an arbitrary entry. ‘1’ as indicated are the leading 1s.

- Rank 3 ones:

$$\begin{bmatrix} \boxed{1} & \boxed{0} & \boxed{0} & \boxed{*} & \boxed{*} & \boxed{*} \\ \boxed{0} & \boxed{1} & \boxed{0} & \boxed{*} & \boxed{*} & \boxed{*} \\ \boxed{0} & \boxed{0} & \boxed{1} & \boxed{*} & \boxed{*} & \boxed{*} \end{bmatrix}$$

$$\begin{bmatrix} \boxed{1} & \boxed{0} & \boxed{*} & \boxed{0} & \boxed{*} & \boxed{*} \\ \boxed{0} & \boxed{1} & \boxed{*} & \boxed{0} & \boxed{*} & \boxed{*} \\ \boxed{0} & \boxed{0} & \boxed{0} & \boxed{1} & \boxed{*} & \boxed{*} \end{bmatrix}$$

$$\begin{bmatrix} \boxed{1} & \boxed{0} & \boxed{*} & \boxed{*} & \boxed{0} & \boxed{*} \\ \boxed{0} & \boxed{1} & \boxed{*} & \boxed{*} & \boxed{0} & \boxed{*} \\ \boxed{0} & \boxed{0} & \boxed{0} & \boxed{0} & \boxed{1} & \boxed{*} \end{bmatrix}$$

$$\begin{bmatrix} \boxed{1} & \boxed{0} & \boxed{*} & \boxed{*} & \boxed{*} & \boxed{0} \\ \boxed{0} & \boxed{1} & \boxed{*} & \boxed{*} & \boxed{*} & \boxed{0} \\ \boxed{0} & \boxed{0} & \boxed{0} & \boxed{0} & \boxed{0} & \boxed{1} \end{bmatrix}$$

$$\begin{bmatrix} \boxed{1} & \boxed{*} & \boxed{0} & \boxed{0} & \boxed{*} & \boxed{*} \\ \boxed{0} & \boxed{0} & \boxed{1} & \boxed{0} & \boxed{*} & \boxed{*} \\ \boxed{0} & \boxed{0} & \boxed{0} & \boxed{1} & \boxed{*} & \boxed{*} \end{bmatrix}$$

$$\begin{bmatrix} \boxed{1} & \boxed{*} & \boxed{0} & \boxed{*} & \boxed{0} & \boxed{*} \\ \boxed{0} & \boxed{0} & \boxed{1} & \boxed{*} & \boxed{0} & \boxed{*} \\ \boxed{0} & \boxed{0} & \boxed{0} & \boxed{0} & \boxed{1} & \boxed{*} \end{bmatrix}$$

$$\begin{bmatrix} \boxed{1} & \boxed{*} & \boxed{0} & \boxed{*} & \boxed{*} & \boxed{0} \\ \boxed{0} & \boxed{0} & \boxed{1} & \boxed{*} & \boxed{*} & \boxed{0} \\ \boxed{0} & \boxed{0} & \boxed{0} & \boxed{0} & \boxed{0} & \boxed{1} \end{bmatrix}$$

$$\begin{bmatrix} \boxed{1} & \boxed{*} & \boxed{*} & \boxed{0} & \boxed{0} & \boxed{*} \\ \boxed{0} & \boxed{0} & \boxed{0} & \boxed{1} & \boxed{0} & \boxed{*} \\ \boxed{0} & \boxed{0} & \boxed{0} & \boxed{0} & \boxed{1} & \boxed{*} \end{bmatrix}$$

- Rank 3 ones (Continued)

1	*	*	*	0	0
0	0	0	0	1	0
0	0	0	0	0	1

0	1	0	*	0	*
0	0	1	*	0	*
0	0	0	0	1	*

0	1	*	0	0	*
0	0	0	1	0	*
0	0	0	0	1	*

0	1	*	*	0	0
0	0	0	0	1	0
0	0	0	0	0	1

0	0	1	0	*	0
0	0	0	1	*	0
0	0	0	0	0	1

0	0	0	1	0	0
0	0	0	0	1	0
0	0	0	0	0	1

- Rank 2 ones:

1	0	*	*	*	*
0	1	*	*	*	*
0	0	0	0	0	0

1	*	0	*	*	*
0	0	1	*	*	*
0	0	0	0	0	0

1	*	*	0	*	*
0	0	0	1	*	*
0	0	0	0	0	0

1	*	*	*	0	*
0	0	0	0	1	*
0	0	0	0	0	0

1	*	*	*	*	0
0	0	0	0	0	1
0	0	0	0	0	0

0	1	0	*	*	*
0	0	1	*	*	*
0	0	0	0	0	0

0	1	*	0	*	*
0	0	0	1	*	*
0	0	0	0	0	0

0	1	*	*	0	*
0	0	0	0	1	*
0	0	0	0	0	0

0	1	*	*	*	0
0	0	0	0	0	1
0	0	0	0	0	0

0	0	1	0	*	*
0	0	0	1	*	*
0	0	0	0	0	0

0	0	1	*	0	*
0	0	0	0	1	*
0	0	0	0	0	0

0	0	1	*	*	0
0	0	0	0	0	1
0	0	0	0	0	0

- Rank 2 ones (Continued)

0	0	0	1	0	*
0	0	0	0	1	*
0	0	0	0	0	0

0	0	0	1	*	0
0	0	0	0	0	1
0	0	0	0	0	0

0	0	0	0	1	0
0	0	0	0	0	1
0	0	0	0	0	0

- Rank 1 ones:

1	*	*	*	*	*
0	0	0	0	0	0
0	0	0	0	0	0

0	1	*	*	*	*
0	0	0	0	0	0
0	0	0	0	0	0

0	0	1	*	*	*
0	0	0	0	0	0
0	0	0	0	0	0

0	0	0	1	*	*
0	0	0	0	0	0
0	0	0	0	0	0

0	0	0	0	1	*
0	0	0	0	0	0
0	0	0	0	0	0

0	0	0	0	0	1
0	0	0	0	0	0
0	0	0	0	0	0

- Rank 0 one:

0	0	0	0	0	0
0	0	0	0	0	0
0	0	0	0	0	0